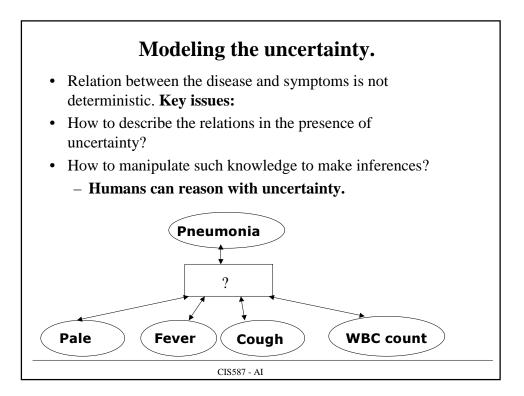


### Uncertainty

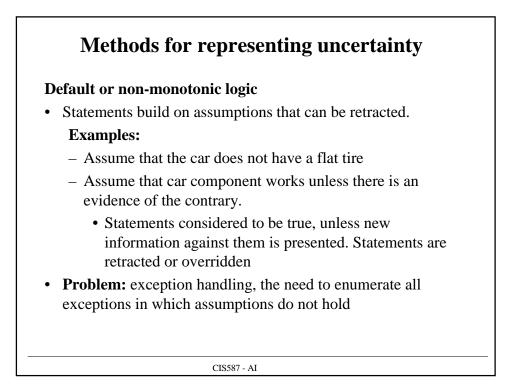
To make diagnostic inference possible we need to represent rules or axioms that relate symptoms and diagnosis

**Problem:** disease/symptoms relation is not deterministic (things may vary from patient to patient) – it is **uncertain** 

- Disease --> Symptoms uncertainty
  - A patient suffering from pneumonia may not have fever all the times, may or may not have a cough, white blood cell test can be in a normal range.
- Symptoms → Disease uncertainty
  - High fever is typical for many diseases (e.g. bacterial diseases) and does not point specifically to pneumonia
  - Fever, cough, paleness, high WBC count combined do not always point to pneumonia



## Uncertainty Relations at the level of detail we consider are not deterministic, they are uncertain Reasons for uncertainty and the need to handle it: Efficiency, capacity limits It is often impossible to enumerate and model all components of the world and their relations Observability It is impossible to observe all relevant components of the world. Humans can reason with uncertainty!!! Can computer systems do the same? We need formalisms to model and manipulate uncertainty.



### Methods for representing uncertainty

Extend formalisms based on propositional and first-order logic to reflect uncertain, imprecise statements (relations)

- Typically rules with various fudge factors
- Popular in 70-80s in knowledge-based systems (e.g., MYCIN)
  - 1. The stain of the organism is gram-positive, and
    - 2. The morphology of the organism is coccus, and
  - 3. The growth conformation of the organism is chains

### Then with certainty 0.7

the identity of the organism is streptococcus

### **Problems:**

If

- Chaining of multiple inference rules (propagation of uncertainty)
- Combinations of rules with the same conclusions
- After some number of combinations results not intuitive

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## Representing uncertainty with certainty factors

- Facts (propositional statements) are assigned some certainty number reflecting the belief in that the statement is satisfied: CF(Pneumonia = True) = 0.7
- Rules incorporate tests on the certainty values

$$(A \text{ in } [0.5,1]) \land (B \text{ in } [0.7,1]) \rightarrow C \text{ with } CF = 0.8$$

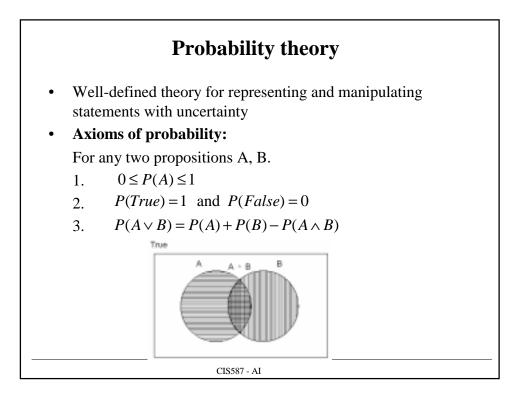
- Combination of multiple rules
  - $(A \text{ in } [0.5,1]) \land (B \text{ in } [0.7,1]) \rightarrow C \text{ with } CF = 0.8$
  - $(E \text{ in } [0.8,1]) \land (D \text{ in } [0.9,1]) \rightarrow C \text{ with } CF = 0.9$

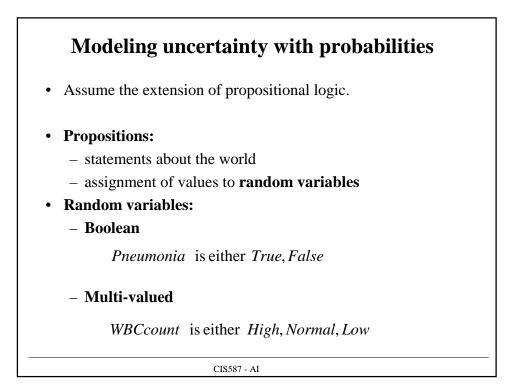
 $CF(C) = \max[0.9; 0.8] = 0.9$ CF(C) = 0.9 \* 0.8 = 0.72

?

CF(C) = 0.9 + 0.8 - 0.9 \* 0.8 = 0.98

# Methods for representing uncertainty Probability theory Proposition statements – represented by random variables and the assignment of (two or more) values to variables Each value can be achieved with some probability: P(Pneumonia = True) = 0.001 P(WBCcount = high) = 0.005 Can model the effect of findings: P(Pneumonia=True| Fever=True) = 0.02 P(Pneumonia=True| Fever=True, WBCcount=high, Cough=True) = 0.4 Subjective (or Bayesian) probability: • Probabilities relate propositions to one own state of knowledge, and not assertions about the world.

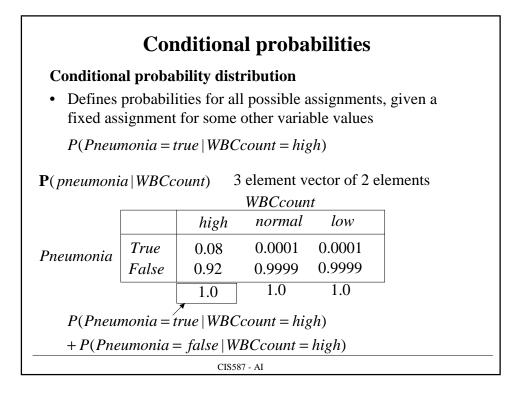


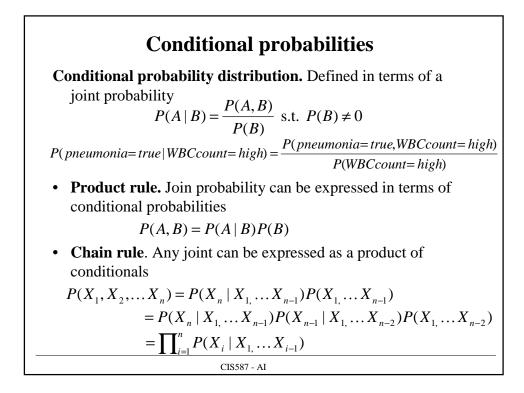


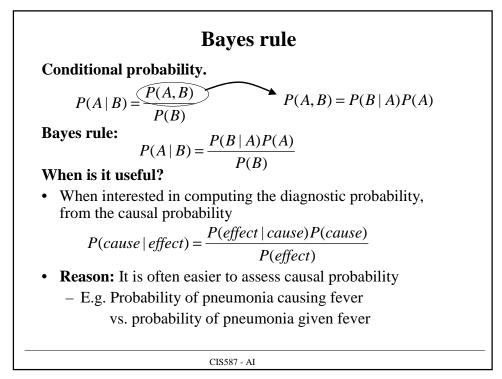
Probabilities							
<b>Unconditional probabilities (prior probabilities)</b> P(Pneumonia) = 0.001 or $P(Pneumonia = True) = 0.001$							
P(WBCcount = high) = 0.005							
Probability distribution	Probability distribution						
• Defines probability values for all possible assignments							
$P(B_{1}, a_{1}, a_{2}, a_{3}, a_{3}$	Pneumonia	<b>P</b> ( <i>Pneumonia</i> )					
P(Pneumonia = True) = 0.001	True	0.001					
P(Pneumonia = False) = 0.999	False	0.999					
– Probabilities sum to 1 !!!							
P(Pneumonia = True) + P(Pneumonia = False) = 1							
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Probability distribution							
<ul><li>Probability distribution</li><li>Defines probability values for all possible assignments</li></ul>							
P(WBCcount = high) = 0.0 $P(WBCcount = normal) =$ $P(WBCcount = high) = 0.0$ Joint probability distribution	WBCcc hig norm low	h nal ,	P(WBCcount) 0.005 0.993 0.002 les)				
<ul> <li>Defines probabilities for variables in the set</li> <li>P(pneumonia,WBCcount)</li> </ul>	ble assignments to values of WBCcount high normal low						
Pneumonia	True False	0.0008 0.0042	0.00 0.99		0.0001 0.0019		
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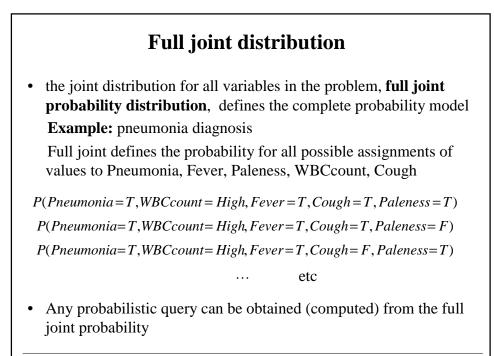
Joint probabilities								
Joint prob	Joint probability distribution (for a set of variables)							
• Defines probabilities for all possible assignments to values of variables in the set								
$\mathbf{P}(pneumonia, WBCcount) = 2 \times 3 \text{ matrix}$								
WBCcount				<b>P</b> ( <i>Pneumonia</i> )				
		high	normal	low				
Pneumonia	True	0.0008	0.0001	0.0001	0.001			
	False	0.0042	0.9929	0.0019	0.999			
	<u></u>	0.005	0.993	0.002				
P(WBCcount)								
Margina	Marginalization (summing of rows, or columns)							
- summing out variables								
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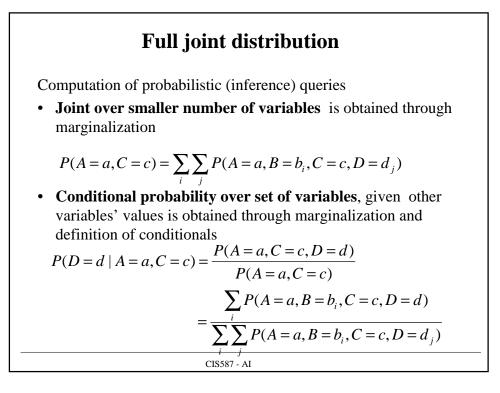


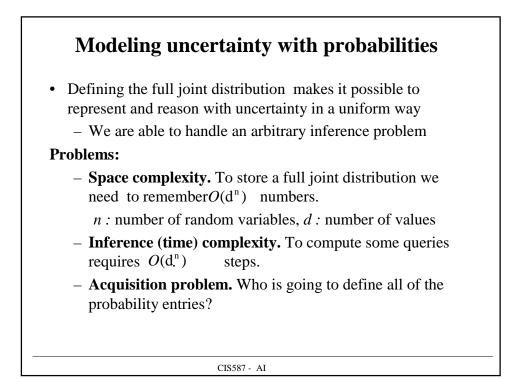


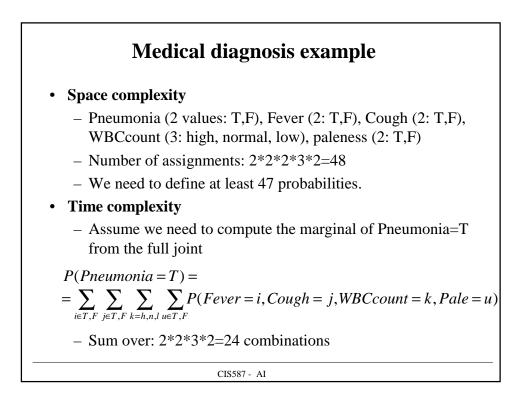


Bayes rule Assume a variable A with multiple values:  $a_1, a_2, ..., a_k$ Bayes rule can be rewritten as:  $P(A = a_j | B = b) = \frac{P(B = b | A = a_j)P(A = a_j)}{P(B = b)}$   $= \frac{P(B = b | A = a_j)P(A = a_j)}{\sum_{i=1}^k P(B = b | A = a_j)P(A = a_j)}$ Used in practice when we want to compute:  $P(A | B = b) \quad \text{for all values of} \quad a_1, a_2, ..., a_k$ 1. compute  $P(B = b | A = a_j)P(A = a_j)$  for all j, and 2. obtain the result by renormalizing the probability vector with  $\beta$  $P(A = a_j | B = b) = \beta P(B = b | A = a_j)P(A = a_j)$   $\beta = 1/\sum_{i=1}^k P(B = b | A = a_j)P(A = a_j)$ 









### Modeling uncertainty with probabilities

- Knowledge based system era (70s early 80's)
  - Extensional non-probabilistic models
  - Space, time and acquisition bottlenecks in probabilitybased models froze the development and advancement of KB systems and contributed to the slow-down of AI in 80s in general
- Breakthrough (late 80s, beginning of 90s)
  - Bayesian belief networks
    - Give solutions to the space, acquisition bottlenecks
    - Partial solutions for time complexities